

Please show your work for all problems. If your work is not present, no partial credit will be given in the case of incorrect answers.

1. (4 points) Identify each of the following as inductive or deductive reasoning.
 - a. All freshmen must live on campus, Joe is a freshman, therefore Joe must live on campus.
Deductive, (General rule, all freshmen must live on campus, to specific conclusion)
 - b. Historical data shows that a person with a college education will earn an average of \$0.9 million more than someone with just a high school education, therefore you should complete your degree.
Inductive (many observations, you make more if you get a degree, to general rule)
 - c. All books by Stephen King have made the best-seller list, *Carrie* is a novel by Stephen King, therefore *Carrie* is a best seller.
Deductive, (General rule about all novels written applied to a novel that has been written)
 - d. All books by Stephen King have made the best-seller list, Stephen King is writing a new novel, this novel will be a best-seller.
Inductive (Observation of all novels written, predicting future behavior)
2. (2 points) Provide a counter-example for each:
 - a. If a number is multiplied by itself, the result is even.
 $1 \times 1 = 1$, which is odd
 - b. The sum of two single digit numbers is a two digit number (ex $5+8 = 13$).
 $1+1 = 2$ which is a single digit number
3. (6 points) Find the next item in the following sequences and state the conjecture you used to determine this number.
 - a. 1, 2, 1, 4, 1, 8, 1, 16, 1, 32
For odd numbers use 1, for even, double the previous even number starting at 2
 - b. 64, -16, 4, -1, 1/4
Multiply the previous number by -1/4
 - c. line, triangle, square,
Any answer is acceptable for this question. I messed up.
4. (4 points) Use deductive reasoning to show that the procedure produces the original number. Select a number, multiply it by 4, add 8 to the product, divide this sum by 2 and subtract 4 from the result, divide the result by 2.
*Let n be the number, (multiply by 4) $4n$, (add 8) $4n+8$
(divide by 2) $(4n+8)/2 = 2n+4$
(subtract 4) $2n+4-4 = 2n$
(divide by 2) $2n/2 = n$*

5. (4 points) In 2004, Microsoft settled a class action lawsuit in California for \$1.1 billion in benefits to consumers. If there were 21,982,341 consumers claiming damages, estimate the amount each consumer was paid. (Please show your work and explain what you did)

Round \$1.1 billion to 1 billion, Round 21 million to 20 million
 $\$1,000,000,000/20,000,000 = 100/2 = \50

6. (4 points) You lease a car for \$605 per month for 4 years, estimate the total cost of the lease.

Round \$605 to \$600

$\$600 \quad 12 \text{ months}$
 $\text{-----} \quad \times \text{-----} \quad \times 4 \text{ years} = 600 \times 12 \times 4 = \$28,800 \quad (\text{but } \$30,000 \text{ was fine})$
 $1 \text{ month} \quad 1 \text{ year}$

7. (4 points) Estimate the salary of a worker who works 78 hours at \$6.87 per hour.

Round 78 to 80 and \$6.87 to \$7

$\$7 \times 80 = \560

8. (4 points) A parking garage charges \$2.50 for the first hour and \$.50 for each additional hour. A customer with a \$5, \$10 and two \$20 bills gives the attendant one of the \$20 bills for parking from 10 am to 3 pm. The attendant spent \$3.50 on lunch, while the customer spent \$50.25 for a pair of shoes. What was the charge for parking?

Find out hours in garage

10 - 11 (1 hour) 2.50

11 - 12 (1 hour) .50

12 - 1 (1 hour) .50

1 - 2 (1 hour) .50

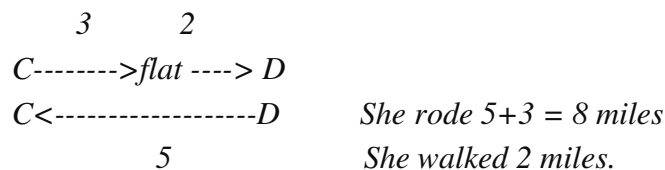
2 - 3 (1 hour) .50

Total: \$2.50 + \$2.00 = \$4.50

9. (4 points) At the beginning of the year, an odometer on a car reads 25,124. At the end of the year it reads 37,364. If the car averages 24 miles per gallon, and gas averages \$2.35 per gallon, how much was spent on gas during the year?

$$\begin{array}{r}
 \text{Total miles: } 37,364 \\
 -25,124 \\
 \hline
 12,240
 \end{array}
 \quad
 \begin{array}{l}
 12,240 \text{ miles} \times \frac{1 \text{ gallon}}{24 \text{ miles}} \times \frac{\$2.35}{1 \text{ gallon}} = 12,240 \times 2.35 / 24 = \$1,198.50
 \end{array}$$

10. (4 points) Charlene decided to ride her bike from home to visit her friend Dan. Three miles away from home, her bike got a flat tire, and she had to walk the remaining two miles to Dan's house. They repaired her tire and she rode back home. How many miles did she walk and how many miles did she ride?



11. (4 points) A farmer has 17 sheep. All but 12 died. How many are left alive?

12.

You might consider this a trick question, but it is from the box on page 29.

12. (4 points) Describe the process of dimensional analysis. Demonstrate this process by converting 450,000 seconds into days.

Any reasonable answer accepted for the first part.

$$450,000 \text{ seconds} \times \frac{1 \text{ min}}{60 \text{ seconds}} \times \frac{1 \text{ hour}}{60 \text{ min}} \times \frac{1 \text{ day}}{24 \text{ hours}} = \frac{450,000}{60 \times 60 \times 24} = 5.2 \text{ days}$$

13. (8 points) 1 mile = 1.6 km.

a. Convert 776 km to mi.

$$776 \cancel{\text{km}} \times \frac{1 \text{ mile}}{1.6 \cancel{\text{km}}} = \frac{776}{1.6} = 485 \text{ miles}$$

b. Convert 23 mi to km.

$$23 \cancel{\text{mi}} \times \frac{1.6 \text{ km}}{1 \cancel{\text{mi}}} = 23 \times 1.6 = 36.8 \text{ km}$$

c. Convert 65 mi/hour to km/hour.

$$\frac{65 \cancel{\text{mi}}}{\text{hour}} \times \frac{1.6 \text{ km}}{1 \cancel{\text{mi}}} = \frac{65 \times 1.6 \text{ km}}{\text{hour}} = 104 \text{ kmph}$$

d. How long, in miles, is a 5 km race?

$$5 \cancel{\text{km}} \times \frac{1 \text{ mi}}{1.6 \cancel{\text{km}}} = 3.12 \text{ mi}$$

14. (4 points) 1 rod is about 5.5 yards. 1 mile is about 8 furlongs. 1 mile is 5280 feet. How many rods in a furlong?

$$1 \text{ furlong} \times \frac{1 \text{ mile}}{8 \text{ furlongs}} \times \frac{5280 \cancel{\text{ft}}}{1 \cancel{\text{mile}}} \times \frac{1 \cancel{\text{yd}}}{3 \cancel{\text{ft}}} \times \frac{\text{rod}}{5.5 \cancel{\text{yd}}} = \frac{5280}{8 \times 3 \times 5.5} = 40 \text{ rod}$$

15. (4 points) If you jog 6 times around a 700 meter track, how many miles have you jogged?

$$\text{Total Distance } 6 \times 700 = 4200 \text{ meters}$$

$$1000 \text{ m} = 1 \text{ km}$$

$$4200 \cancel{\text{m}} \times \frac{1 \cancel{\text{km}}}{1000 \cancel{\text{m}}} \times \frac{1 \text{ mile}}{1.6 \cancel{\text{km}}} = \frac{4200}{1000 \times 1.6} \text{ miles} = 2.6 \text{ miles.}$$

16. (4 points) 1 cubit = 1.5 foot. 1 foot = 30.5 cm. 1 kiloliter (kL) = 1 m³. In the Bible, Noah built an ark that was 300 cubits long by 50 cubits wide by 30 cubits tall. Find the volume of the ark in kL.

$$V = l \times w \times h \quad V = 300 \times 50 \times 30 = 450,000 \text{ cubits}^3$$

$$450000 \text{ cubits}^3 \times \frac{1.5 \text{ ft}}{\text{cubit}} \times \frac{1.5 \text{ ft}}{\text{cubit}} \times \frac{1.5 \text{ ft}}{\text{cubit}} \times \frac{30 \text{ cm}}{\text{ft}} \times \frac{30 \text{ cm}}{\text{ft}} \times \frac{30 \text{ cm}}{\text{ft}} \times \frac{1 \text{ m}}{100 \text{ cm}} \times \frac{1 \text{ m}}{100 \text{ cm}} \times \frac{1 \text{ m}}{100 \text{ cm}} \times \frac{\text{kL}}{\text{m}^3} = 41,006 \text{ kL}$$

Ok, so this one was hard, you needed to keep everything straight to make it through this.

17. (4 points) A square inch of property on the moon sells for \$100. Find the price per acre. (1 acre is about 4820 square yards)

$$\frac{\$100}{\text{in}^2} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{3 \text{ ft}}{1 \text{ yd}} \times \frac{3 \text{ ft}}{1 \text{ yd}} \times \frac{4820 \text{ yd}^2}{\text{acre}} = \frac{\$624,672,000}{\text{acre}}$$

18. (4 points) Convert 140 mL to kL.

kilo
 hecto
 deka
 -
 deci
 centi
 mili

$$140 \text{ mL} \times \frac{1 \text{ kL}}{1000000 \text{ mL}} = .00014 \text{ KL}$$

19. (4 points) Convert 3.7 dg to dag.

$$100 \text{ dg} = 1 \text{ dag}$$

$$3.7 \text{ dg} \times \frac{1 \text{ dag}}{100 \text{ dg}} = .037 \text{ dag}$$